

ALIGNMENT OF PROTOSTARS AND CIRCUMSTELLAR DISKS DURING THE EMBEDDED PHASE

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ABSTRACT

Star formation proceeds via the collapse of a molecular cloud core over multiple dynamical timescales. Turbulence within cores results in a spatially non-uniform angular momentum of the cloud, causing a stochastic variation in orientation of the disk forming from the collapsing material. In the absence of star-disk angular momentum coupling, such disk-tilting would provide a natural mechanism for production of primordial spin-orbit misalignments in the resulting planetary systems. However, owing to high accretion rates in the embedded phase of star formation, the inner edge of the circumstellar disk extends down to the stellar surface, resulting in efficient gravitational and accretional angular momentum transfer between the star and the disk. Here, we demonstrate that the resulting gravitational coupling is sufficient to suppress any significant star-disk misalignment, with accretion playing a secondary role. The joint tilting of the star-disk system leads to a stochastic wandering of star-aligned bipolar outflows. Such wandering widens the effective opening angle of stellar outflows, allowing for more efficient clearing of the remainder of the protostar's gaseous envelope. Accordingly, the processes described in this work provide an additional mechanism responsible for sculpting the stellar Initial Mass Function (IMF).

1. INTRODUCTION

In the simplest picture for star and planet formation, the angular momentum vectors for stellar rotation, the circumstellar disk, and the resulting planetary orbits all coincide. However, recent observations showing that planetary orbits are often misaligned with stellar rotation axes (Fabrycky & Winn 2009; Winn et al. 2010) have prompted several authors (e.g. Bate et al. 2010; Batygin 2012) to suggest that disks themselves may become misaligned with their parent stars. Any such primordial star-disk misalignment occurring within the embedded phase, during which the star gains most of its mass, has consequences both for future planetary systems and for the impact of protostellar outflows on their surrounding envelopes. In this Letter, we construct a model for protostar-disk systems that describes the gravitationally-facilitated precession of the stellar rotation axis about a tilting disk, including dissipative torques owing to accretion.

In spite of enormous progress in our understanding of star formation (from Shu et al. 1987b to McKee & Ostriker 2007), the final mass of a star still cannot be unambiguously determined from the initial conditions of the original molecular cloud core. Protostellar outflows represent one mechanism that can help separate a newly formed star from its immediate environment (Shu et al. 1987b), and this mechanism may provide an explanation for the stellar initial mass function (Adams & Fatuzzo 1996). Although outflows have sufficient mechanical luminosity to reverse the infall (Lada 1985), one criticism of this picture is that the outflows start with relatively narrow angular extents. However, the opening angles widen with time and precessing outflows can produce

outflow cones that are effectively wider than their intrinsic extent, thereby making it easier for outflows to limit the mass falling onto the central star/disk system. Independent of the efficacy of the outflows in limiting stellar masses, observations show that protostellar jets precess (Eisloffel et al. 1996; Cesaroni et al. 2005) and that circumstellar disks are not always aligned with the plane of binary orbits (Stapelfeldt et al. 1998; Koresko 1998).

The angular momentum of a circumstellar disk must be obtained from the gradual accumulation of material from a molecular cloud core. Rotation rates of such cores are estimated through measurements of velocity gradients of a given molecular line across the map of the core (e.g., Goodman et al. 1993). The inferred angular velocity vectors *do not point in the same direction over the entire core*; instead they vary in projected direction over a range of ~ 30 degrees within the region encompassing material that is destined to form a star. Moreover, the coherence length λ for the velocity vectors inferred from these emission maps is $\lambda \sim 0.01$ pc (Caselli et al. 2002). As collapse of these core structures proceeds, the infalling material will thus sample cloud layers of differing angular momentum orientation. As the layers fall inward and join the growing star/disk system, the angular momentum vector of the system must vary in direction (as well as magnitude). On a related note, these cores are observed to be turbulent, especially in the outer layers of low-mass cores (Myers & Fuller 1992) and in more massive cores (Jijina et al. 1999). The collapse of a turbulent region also produces varying directions for the angular momentum vectors of the forming star/disk systems as the collapse proceeds. Numerical simulations of this process (Bate et al. 2010; Fielding et al. 2014) show that the angular momentum vectors of the disks change as different cloud layers fall inward.

Assuming the star to be decoupled from the disk, star-disk misalignment is indeed an expected result of disk-tilting. However, young stars rotate rapidly, becoming oblate. This oblateness leads to a gravitationally-forced precession of the stellar spin axis with respect to the disk (Batygin & Adams 2013) and provides a physical mechanism by which the star's spin axis may trail the disk as it tilts. Additional potential sources of stellar spin-axis evolution include accretion, stellar winds and magnetic fields. As we are considering the Class 0 phase, accretion is likely to dominate over other effects, as discussed below.

2. MODEL DESCRIPTION

We begin by describing the basic model, illustrated in Figure 1, whereby a molecular cloud core collapses to form a star and circumstellar disk. As noted in the Introduction, sequential radii within the core differ in mean angular momentum direction. Owing to the large angular momentum reservoir of the collapsing material, the disk will in turn adopt a time-varying orientation as the core collapses onto it. Within the physical framework considered here, there exist three relevant timescales. Specifically, these are the shell-shell de-correlation time (τ_{dc}), the characteristic star-disk realignment time (τ_{r}) and the nodal regression period of the stellar spin-axis (T). Let us evaluate these quantities sequentially.

2.1. Turbulent Core Collapse

Although the detailed structure of the core is complicated, we assume that the density distribution has the form

$$\rho(r) = \frac{A c_s^2}{2\pi G r^2}, \quad (1)$$

where c_s is the isothermal sound speed and $A > 1$ is an overdensity factor (Fatuzzo et al. 2004) that accommodates the fact that cores are not in exact hydrostatic equilibrium (Lee et al. 1999). With the density distribution (1), the enclosed mass has the form

$$M(r) = \frac{2 A c_s^2 r}{G}. \quad (2)$$

Motivated by both observations of emission maps (Caselli et al. 2002) and numerical simulations of collapsing turbulent cores (Bate et al. 2010; Fielding et al. 2014), we assume that different (spherical) shells have different directions for their angular velocity. To be consistent with observed maps and numerical expectations, the shell thickness should be comparable to, but smaller than, the coherence length λ . For the sake of definiteness, we take the shell thickness $\ell = \lambda/2 = 0.005$ pc. With this choice, the formation of a solar type star will involve the collapse of $N = 5 - 10$ shells. The mass of each shell is given by

$$\Delta m = \frac{2 A c_s^2}{G} \ell \approx 0.10 M_{\odot} \left(\frac{c_s}{0.2 \text{ km/s}} \right)^2 \left(\frac{\ell}{0.005 \text{ pc}} \right). \quad (3)$$

Each of these shells is then assumed to have an angular velocity vector with direction chosen randomly within a range $0 - 30$ degrees. In this scenario, the mass infall rate is nearly constant with $\dot{M} = m_0 c_s^3 / G$, where m_0 is a dimensionless constant of order unity (Shu 1977). The

shell-shell decorrelation time is equal to the corresponding time interval required for a shell to fall inward, given by

$$\tau_{\text{dc}} = \frac{2A}{m_0} \frac{\ell}{c_s} \approx 25,000 \text{ yr}. \quad (4)$$

In order to model angular velocity variation, we define scaled Poincaré action-angle coordinates in terms of inclination angle β and longitude of ascending node Ω :

$$\mathcal{Z} = 1 - \cos(\beta) \quad z = -\Omega. \quad (5)$$

We randomly choose the third Poincaré momentum of shell i from a Gaussian distribution having mean $\mu = \mathcal{Z}_{i-1}$ and standard deviation $\sigma = \mathcal{Z}_{30^\circ}$ where $\mathcal{Z}_{30^\circ} = 1 - \cos(30^\circ)$ is the value of $\mathcal{Z}_{\text{disk}}$ corresponding to a 30 degree inclination. Specifically,

$$\mathcal{Z}_{i+1} = \mathcal{R}_{\text{an}} \left[\exp \left(- \frac{(\mathcal{Z} - \mathcal{Z}_i)^2}{2\mathcal{Z}_{30^\circ}^2} \right) \right], \quad (6)$$

where $\mathcal{R}_{\text{an}}[\]$ symbolises extracting a random number from the distribution within parentheses. Likewise, the canonical angle z of shell i relative to shell $i - 1$ is drawn randomly, but from a uniform distribution of $0 \leq -z \leq 2\pi$. Additional, small-scale turbulence-mediated stochasticity is introduced by way of 100 N smaller shells, each varying in a Gaussian form by a value of 1 degree. Once all shells have been prescribed a value of \mathcal{Z} and z , we smooth the 100 N inclinations into a continuous function of time by considering the entire star formation process to proceed over a time $\tau_{\text{form}} = 2 \times 10^5$ years and thus, for each of the 100 N inclinations to occur within a time interval of $\Delta t = \tau_{\text{form}}/100 N$. Using a 3rd order cubic spline interpolation, we generate a pseudo-random function of time, $\{\mathcal{Z}(t), z(t)\}$, denoting the time-varying angular momentum vector of the collapsing material. Assuming the disk to obtain its angular momentum directly from the envelope, the disk angular momentum vector instantaneously follows that of the collapsing shells.

2.2. Realignment Time

The angular momentum of a rotating star is given by the well-known expression

$$\mathcal{L}_{\star} = I M_{\star} R_{\star}^2 \omega, \quad (7)$$

where I is the dimensionless moment of inertia and ω is the stellar spin. For the purposes of this Letter, we shall adopt stellar structure parameters corresponding to $n = 3/2$ polytrope, which corresponds to a fully convective object.

At the earliest stages of stellar evolution, accretion rates of disk material onto the protostellar core can be ubiquitously high with characteristic values of order $\dot{M} \sim 10^{-5} M_{\odot}/\text{yr}$ (for a $M \sim 1 M_{\odot}$ object; see Ward-Thompson 2002). Accordingly, the accretionary ram pressure may in fact be sufficient to overwhelm the magnetic pressure of the protostellar magnetosphere, connecting the disk's inner edge to the stellar surface (Ghosh & Lamb 1978). The critical magnetic field strength, B_{crit} , below which this happens can be estimated by setting the magnetospheric disk truncation radius to that

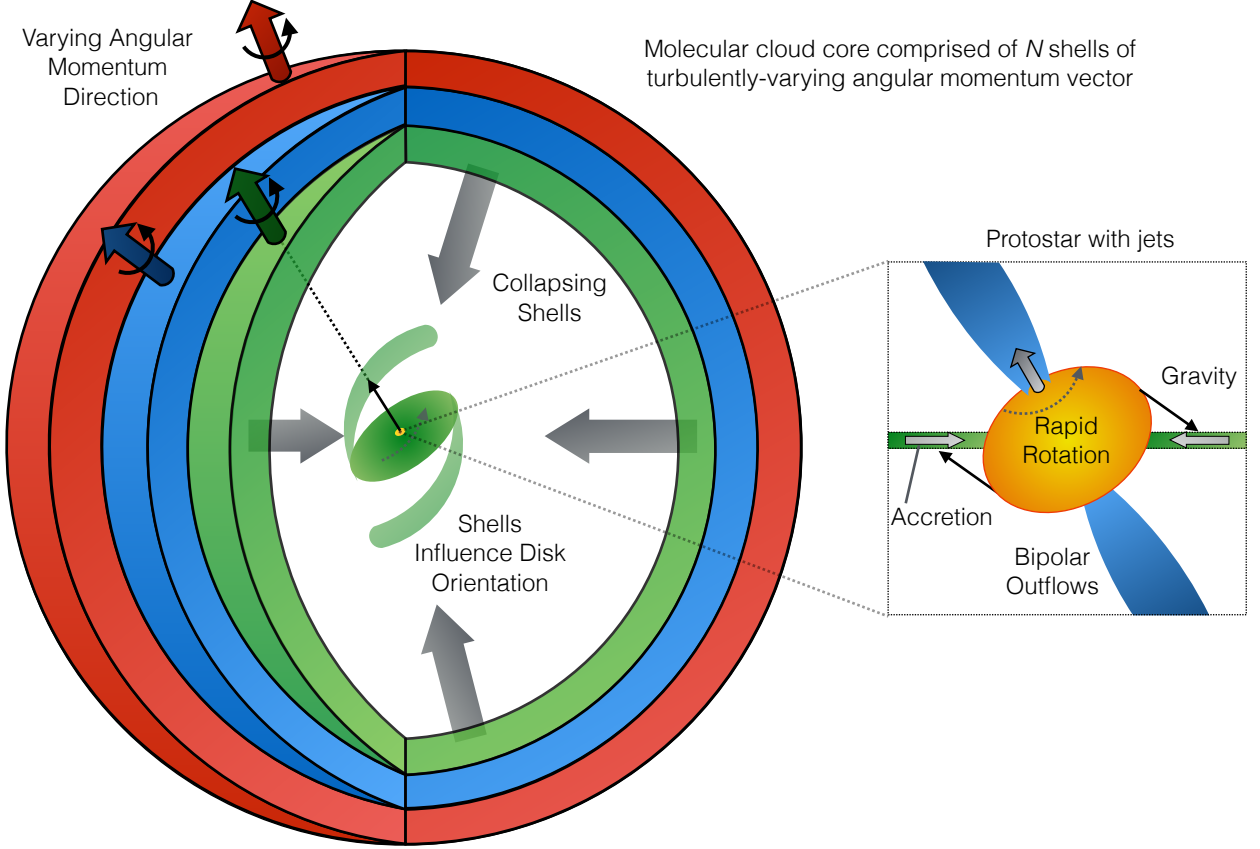


FIG. 1.— A schematic of the process described in the text. Different shells possess different angular momentum vectors. In turn, the disk changes its orientation with time. Gravitational and accretional torques act between the star and disk, with bipolar outflows originating from the stellar spin axis.

of the star (Shu et al. 1994):

$$B_{\text{crit}} = \left(\frac{G M_{\star} \dot{M}^2 \xi^7}{R_{\star}^5} \right)^{1/4}, \quad (8)$$

where ξ is a dimensionless constant of order unity (Mohanty & Shu 2008). Given nominal parameters, the critical field evaluates to $B_{\text{crit}} \sim 1 \text{ MG}$, which is well above the oft-cited $B_{\star} \sim 1 \text{ kG}$ fields inherent to young stellar objects (Gregory et al. 2012).

In a regime where the inner edge of the disk is physically connected to the stellar surface, the accretionary flow will facilitate a direct and efficient transfer of angular momentum between the disk and the host star (Ghosh & Lamb 1979). While the details of the disk-star coupling in a shearing boundary layer can be complex (Belyaev et al. 2013), to leading order the rate of stellar angular momentum accumulation can be written as follows (Armitage & Clarke 1996):

$$\frac{d\mathcal{L}_{\star}}{dt} \simeq \dot{M} \sqrt{G M_{\star} R_{\star}}. \quad (9)$$

With the above equations at hand, we may now define a characteristic timescale for accretion-forced realignment of the stellar spin-axis. Specifically, we have:

$$\tau_{\text{r}} \equiv \frac{\mathcal{L}_{\star}}{d\mathcal{L}_{\star}/dt} \sim \frac{I M_{\star} R_{\star}^2 \omega}{\dot{M} \sqrt{G M_{\star} R_{\star}}} \sim 10^4 \text{ years}, \quad (10)$$

where as an estimate of the stellar spin rate we adopt the

break-up rotational velocity $\omega = \sqrt{G M_{\star} / R_{\star}^3}$, leading to $\tau_{\text{r}} = I (M_{\star} / \dot{M})$, which is independent of stellar radius, R_{\star} . Note the similarity between τ_{r} and the shell infall timescale (equation 4)

Additional effects can change the alignment. Perhaps most notably, modulation of the stellar spin-axis may arise from magnetic disk-star coupling (Lai et al. 2011; Spalding & Batygin 2014). While we have neglected this effect here, the fact that the accretionary flow at early stages of stellar evolution is intense enough to penetrate the stellar magnetosphere suggests that, indeed, the dominant mode of realignment will be facilitated by accretion and not magnetohydrodynamic effects.

2.3. Precession

As mentioned above, during the Class 0 epoch of stellar formation, young stellar objects may spin at near-breakup velocities. This naturally leads to significant rotational deformation. The spin-axis dynamics of an oblate spheroid can be modeled using standard techniques of celestial mechanics by replacing the rotational bulge of the star with an inertially equivalent orbiting ring of semi-major axis

$$\chi = \left(\frac{16 \omega^2 k_2^2 R_{\star}^6}{9 I^2 G M_{\star}} \right)^3 = R_{\star} \left(\frac{4 k_2}{3 I} \right)^{2/3}, \quad (11)$$

where $k_2 = 0.14$ is the Love number¹ (twice the apsidal motion constant). The second equality follows from assuming that the star spins at breakup frequency. In principle, the aforementioned ring has a well-specified mass, however, its value only controls the back-reaction of the stellar quadrupole moment on the disk, which is unimportant.

To complete the specification of the problem, we must characterize the properties of the disk. We take the disk to be axisymmetric, and its surface density to vary inversely with semi-major axis (Andrews et al. 2010):

$$\Sigma = \Sigma_0 \left(\frac{a}{a_0} \right)^{-1}, \quad (12)$$

where Σ_0 is the surface density at $a = a_0$. Additionally, we take the disk aspect ratio to be $\zeta \equiv h/a = 0.05$, though its actual value likely varies with disk radius up to ~ 0.1 (Armitage 2011). We note that under this prescription,

$$M_{\text{disk}} = \int_0^{2\pi} \int_{R_*}^{a_{\text{out}}} \Sigma a da d\phi \simeq 2\pi \Sigma_0 a_0 a_{\text{out}}, \quad (13)$$

where $a_{\text{out}} = 30 - 50$ AU is the physical size of the disk (Kretke et al. 2012; Anderson et al. 2013).

To compute the dynamical evolution, we make use of classical perturbation theory (Morbideilli 2002). Accordingly, we must first choose the appropriate expansion of the disturbing Hamiltonian. Given that $\chi \approx R_*$ and the inner boundary of the disk is linked to the stellar surface, an expansion in the semi-major axis ratio (Kaula 1962; Spalding & Batygin 2014) is bound to be slowly-convergent. Therefore, in this work we shall opt for an alternative description that assumes mutual disk-star inclination as a small parameter and places no restrictions on the semi-major axis ratio (Le Verrier 1856; Murray & Dermott 1999).

As a starting step, consider the mutual interaction of a massive hoop representing the stellar rotational bulge and a disk annulus of radial thickness da . It is a well-known result of secular perturbation theory that upon averaging over the orbital phase, the semi-major axes of both rings are rendered constants of motion. Thus, the Keplerian contributions to the Hamiltonian become trivial and can be omitted.

To leading order in mutual inclination, the Lagrange-Laplace disturbing Hamiltonian reads (Batygin & Adams 2013):

$$d\mathcal{H} = \frac{\tilde{b}_{3/2}^{(1)}}{4} \sqrt{\frac{\mathcal{G} M_*}{a^3}} \frac{dm}{M_*} \sqrt{\frac{\chi}{a}} \left[\mathcal{Z}_{\text{star}} - 2\sqrt{\mathcal{Z}_{\text{star}} \mathcal{Z}_{\text{disk}}} \cos(z_{\text{star}} - z_{\text{disk}}) \right], \quad (14)$$

where $dm = 2\pi \Sigma_0 a_0 da$ is the mass of the perturbing annulus, $\tilde{b}_{3/2}^{(1)}$ is a softened Laplace coefficient (see below for an explicit expression).

To obtain the Hamiltonian governing the interactions between the star and the full disk, we integrate with

respect to the semi-major axis ratio $\alpha = \chi/a$:

$$\begin{aligned} \mathcal{H} = & \frac{1}{4\pi} \sqrt{\frac{\mathcal{G} M_*}{\chi^3}} \frac{M_{\text{disk}}}{M_*} \frac{\chi}{a_{\text{out}}} \\ & \times \left(\int_0^{\chi/R_*} \int_0^{2\pi} \frac{\cos(\psi)}{(1 - 2\alpha \cos(\psi) + \alpha^2 + \zeta^2)^{3/2}} d\psi d\alpha \right) \\ & \times \left[\mathcal{Z}_{\text{star}} - 2\sqrt{\mathcal{Z}_{\text{star}} \mathcal{Z}_{\text{disk}}} \cos(z_{\text{star}} - z_{\text{disk}}) \right] \end{aligned} \quad (15)$$

Note that in this formulation of the problem, we are not explicitly solving for the dynamical evolution of the disk using the above Hamiltonian. Instead, the time-varying variables $(\mathcal{Z}_{\text{disk}}, z_{\text{disk}})$ constitute prescribed functions of time, as described above. Suitably, the only equations of motion we derive from equation (15) are those corresponding to the $(\mathcal{Z}_{\text{star}}, z_{\text{star}})$ degree of freedom.

Although the inclination, i , and the longitude of ascending node, Ω , are measured in an inertial reference frame, the inherent assumption of the Lagrange-Laplace secular theory is that the *mutual* disk-star inclination remains small (Morbideilli et al. 2012). Thus, it is important to understand that any solution obtained within the framework of this description is only trustworthy if it dictates a low disk-star inclination for the entirety of the time-span of interest. Conversely, if mutual disk-star inclination is to increase to an appreciable value, one must default to the much more computationally expensive, but ultimately precise Gaussian averaging method (Touma et al. 2009).

To obtain the precession rate of the stellar spin axis in the frame of the disk, we may envision that the disk remains stationary at $\beta = 0$ (this assumption will be lifted later), meaning that $\mathcal{Z}_{\text{disk}} = 0$. This puts the amplitude of the harmonic part of the Hamiltonian (15) to zero, such that \mathcal{H} governs pure rotation in z_{star} . Accordingly, we have:

$$\mathcal{T} = 2\pi \left(\frac{\partial \mathcal{H}}{\partial \mathcal{Z}_{\text{star}}} \right)^{-1} \simeq 130 \left(\frac{0.01 M_\odot}{M_{\text{disk}}} \right) \left(\frac{M_*}{1 M_\odot} \right) \text{ years.} \quad (16)$$

For all reasonable choices of parameters, the precession timescale of the stellar spin-axis (which acts as the dynamical timescale of the problem at hand) is substantially shorter than both the accretionary realignment timescale and the shell-shell decoherence timescale. This feature is of crucial importance to understanding the results that follow, as it effectively guarantees that the dynamical evolution occurs within the *adiabatic* regime, within which the star trails the disk's orientation.

3. NUMERICAL SIMULATIONS

Equations of motion arising from Hamiltonian (15), as formulated in terms of action-angle coordinates (5) contain a coordinate singularity at $\mathcal{Z}_{\text{star}} = 0$. This complication can be removed with a canonical change of variables. Specifically, we introduce a complex coordinate

$$\eta = \sqrt{\mathcal{Z}} \cos(z) + i\sqrt{\mathcal{Z}} \sin(z), \quad (17)$$

¹ This value corresponds to a polytropic body of index $n = 3/2$

where $\imath = \sqrt{-1}$. The Hamiltonian now reads:

$$\mathcal{H} = \mathcal{S}(\eta_{\text{star}}\eta_{\text{star}}^* + \eta_{\text{star}}\eta_{\text{disk}}^* + \eta_{\text{star}}^*\eta_{\text{disk}}), \quad (18)$$

where $\mathcal{S} = 2\pi/\mathcal{T}$ is the coefficient on the first line of equation (18) and the asterisk denotes a complex conjugate.

In addition to the dynamical evolution governed by \mathcal{H} , it is important to account for the dissipative effects originating from the realigning influence of accretionary torques, in the equations of motion. For tractability, it is sensible to parameterize such realignment as an exponential decay of the action² $\mathcal{Z}_{\text{star}}$. Cumulatively, the relevant equation of motion takes the form:

$$\begin{aligned} \frac{d\eta_{\text{star}}}{dt} &= \imath \left(\frac{\partial \mathcal{H}}{\partial \eta_{\text{star}}^*} \right) + \left(\frac{d\eta_{\text{star}}}{dt} \right)_{\text{r}} \\ &= \imath \mathcal{S}(\eta_{\text{star}} + \eta_{\text{disk}}) - \frac{\eta_{\text{star}}}{2\tau_{\text{r}}}, \end{aligned} \quad (19)$$

where $(d\eta_{\text{star}}/dt)_{\text{r}}$ describes the dissipative term, which acts to damp any misalignment. Without the dissipative term, equation 19 describes conservative, gravitational precession of the stellar spin axis about a time-varying disk angular momentum vector.

To complete the specification of the problem, we prescribe the time evolution of a $1 M_{\odot}$ star as

$$M_{\text{star}}(t) = M_{\odot} \left(\epsilon + \frac{t}{\tau_{\text{form}}} \right) \quad (20)$$

where $\epsilon = 0.01$ represents a small initial ‘seed’ mass onto which shells collapse. Additionally, the circumstellar disk mass (M_{disk}) grows proportionally to that of the star such that

$$M_{\text{disk}}(t) = 0.1 M_{\text{star}}(t), \quad (21)$$

with the 0.1 prefactor corresponding approximately to the upper limit for dynamical stability (Armitage 2011). We consider a constant stellar radius of $R_{\star} = 4 R_{\odot}$ throughout (Stahler et al. 1980).

4. RESULTS & DISCUSSION

In Figure 2 we present the paths followed by the stellar and disk angular momentum vectors in the purely gravitational regime, i.e., zero accretion. As is immediately obvious, the two paths are indistinguishable, meaning that even in the absence of accretionary realignment, no significant star-disk misalignment can result from turbulent core collapse. Accretionary torques simply act to reduce the already-miniscule misalignments (Figure 3) and so are dynamically unimportant to the problem at hand. As such, the first crucial result is that the *hypothesis that turbulent core-collapse leads to primordial spin-orbit misalignments is inconsistent with the framework presented here*. Spin-orbit misalignments must be obtained at a later evolutionary stage, such as during the main phase of planet formation (Lai et al. 2011; Batygin 2012; Batygin & Adams 2013; Spalding & Batygin 2014) or after the disk has dispersed (e.g., Wu & Lithwick 2011; Beaugé & Nesvorný 2012; Albrecht et al. 2012).

² Introduction of such terms into the equations of motion tends to transform nearby elliptical fixed points into attractors (see e.g. Batygin & Morbidelli 2011).

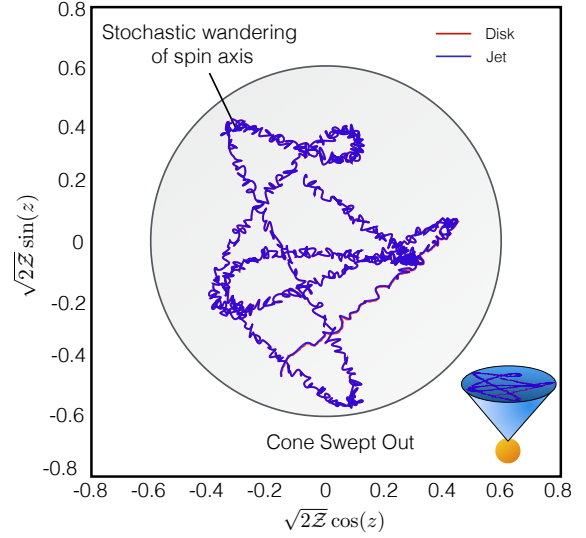


FIG. 2.— The paths traced out by the angular momentum vectors of the disk (red) and star (blue) plotted in canonical Cartesian coordinates (see text). Notice that the red and blue paths almost exactly overlap. The shaded region approximately inscribes the cone of gas cleared out by stellar spin axis-aligned jets.

Class 0 and Class I protostars possess collimated bipolar jets with sufficient mechanical luminosity to reverse the infall of core material. Such jets have been observed to ‘wobble’ in such a way as to suggest time evolution of the jet direction (Eisloffel et al. 1996; Cesaroni et al. 2005). Previous pictures considering only disk motion do not necessarily account for jet wiggles as the jets are collimated along the stellar spin axis through the action of magnetic fields (Shu et al. 1994). Thus the jet itself is unlikely to move significantly if the star itself is not changing orientation. As noted by Shu et al. (1987b), a star breaks free of its enshrouding molecular envelope once outward pressures owing to stellar winds and jets exceed the ram pressure of infalling gas. Stellar outflows contribute significantly to such outward pressures and thus may in part determine the final mass of the forming star. Here we find that the stellar outflows carry out a random walk (Figure 2), leading to an effectively wider opening angle of the outflow. Accordingly, the wandering outflows may help separate the newly formed star/disk system from its environment earlier than would a stationary outflow. Such a physical process adds an important correction onto previous theories of star formation (e.g., Adams & Fatuzzo 1996) which propose that the IMF may be determined in part by outflows.

Here, we considered a constant mass infall rate of $\dot{M} \approx 10^5 M_{\odot} \text{ year}^{-1}$ over the entire star formation process. Strictly speaking, this assumption contradicts the non-steady nature of turbulent collapse. In principle, sufficiently violent episodic mass infall may lead to more rapid variations in disk angular momentum than considered here. However, owing to the vast separation of timescales between shell-shell decorrelation ($\tau_{\text{dc}} \sim 10^4$ years) and stellar precession ($\mathcal{T} \sim 10^2$ years) the star shall trail the disk under almost any reasonable collapse conditions. Additionally, the mass infall and accretion rates fall by about an order of magnitude over a longer

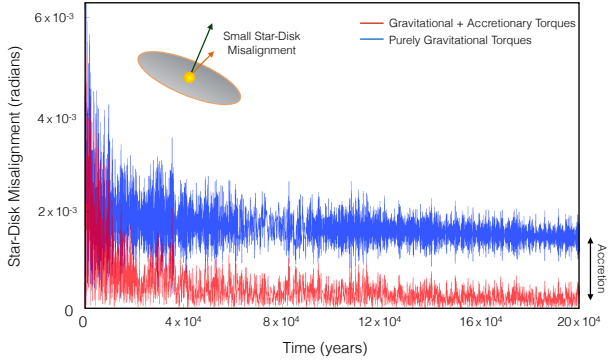


FIG. 3.— The misalignment between star and disk angular momenta plotted as a function of time. Gravitational interactions alone (blue) are sufficient to suppress significant misalignment. Accretionary torques (red) further reduce the misalignment to near-zero values.

timescale, between the Class 0 and Class I phases of star formation (Ward-Thompson 2002). Such a drop in infall rate is not included in our model but during the Class I phase, most of the mass is in the star-disk system (by

definition) and so, combined with a drop in infall rate, disk tilting is likely to become significantly lower in amplitude. Accordingly, the star should remain even more tightly coupled to the disk, despite reduced accretionary torques, which we determined to be dynamically unimportant.

This Letter presents a simple model for star/disk formation in molecular cloud cores possessing non-uniform angular momentum directions. We find that outflows change direction substantially, but stars and disks remain nearly aligned. Future work should develop more detailed models for all aspects of this problem, including the initial conditions, disk formation, wandering of outflow directions and misalignment between star and disk.

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